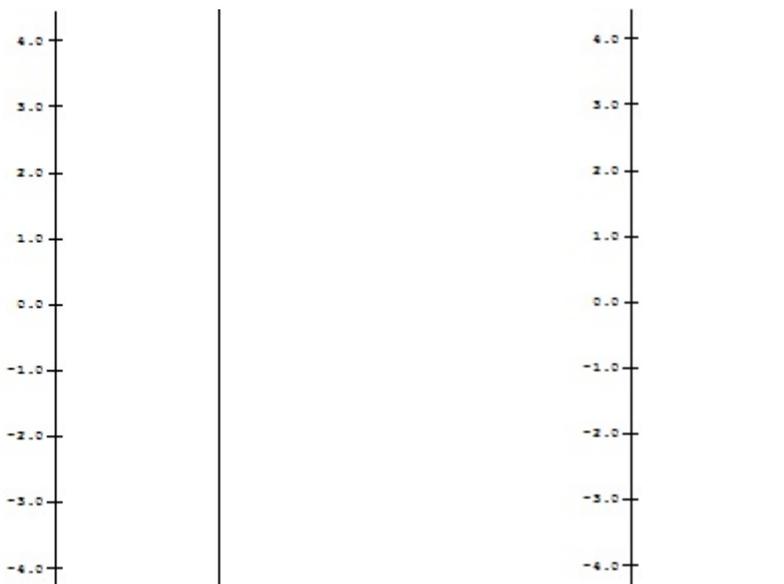


1.

a. Complete the following tables for $m(x) = 2x$ and $s(x) = x + 1$

| x | $m(x) = 2x$ | $s(x) = x + 1$ |
|-----|-------------|----------------|
| 2 | | |
| 1 | | |
| 0 | | |
| -1 | | |
| -2 | | |

b. Using the data from part a), on separate diagrams sketch mapping diagrams for $m(x) = 2x$ and $s(x) = x+1$

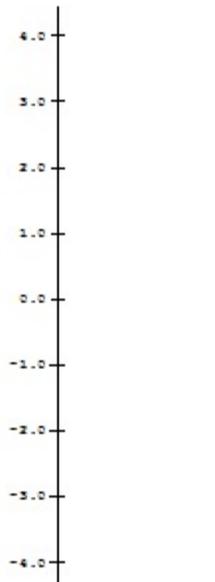


2. Let $q(x) = x^2$.

a. Complete the following table for $q(x) = x^2$.

| x | $q(x) = x^2$ |
|-----|--------------|
| 2 | |
| 1 | |
| 0 | |
| -1 | |
| -2 | |

b. Using the data from part a), sketch a mapping diagram for $q(x) = x^2$.



3.

a. Complete the following table for the composite function $f(x) = s(m(x)) = 2x + 1$.

| x | $m(x) = 2x$ | $s(m(x)) = 2x + 1$ |
|-----|-------------|--------------------|
| 2 | | |
| 1 | | |
| 0 | | |
| -1 | | |
| -2 | | |

b. Use the table and the previous sketches of 1.b to draw a composite sketch of the mapping diagram with 3 axes for the composite function $f(x) = s(m(x)) = 2x + 1$

c. Draw a sketch for the mapping diagram with 2 axes of $f(x) = 2x + 1$.

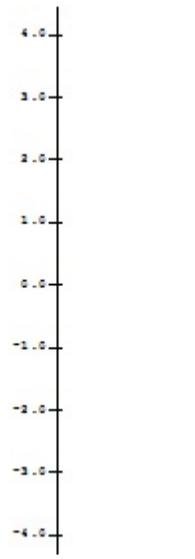
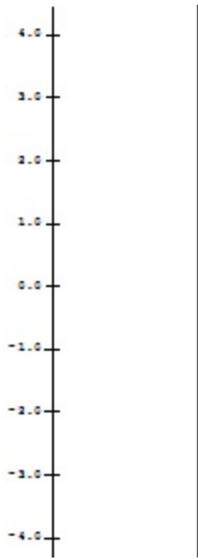


4. Let $f(x) = mx + b$ sketch mapping diagrams for the following:

Use the same scale for the second axis.

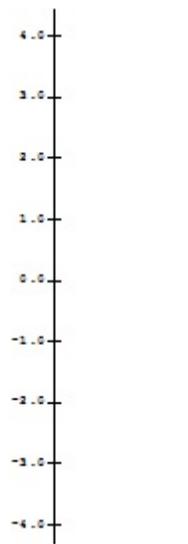
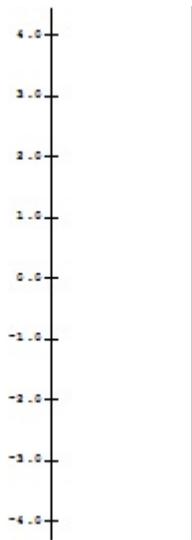
d. $m = 0; b = 1: f(x) = 0x + 1$

a. $m = -2; b = 1: f(x) = -2x + 1;$

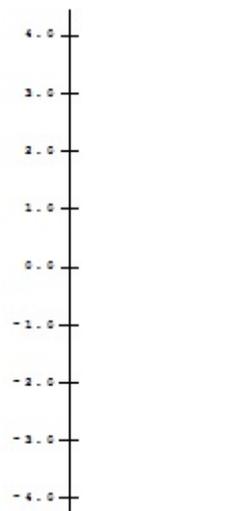


b. $m = 2; b = 1: f(x) = 2x + 1$

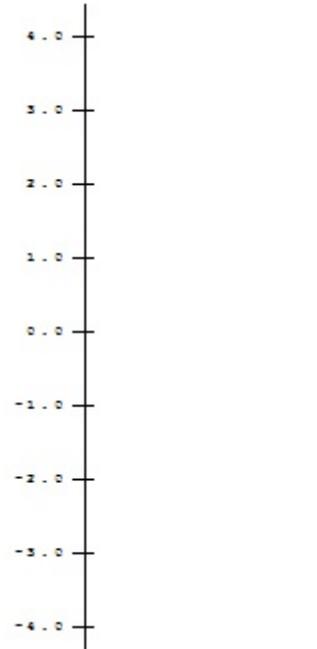
e. $m = 1; b = 1: f(x) = x + 1$



c. $m = \frac{1}{2}; b = 1: f(x) = \frac{1}{2}x + 1$



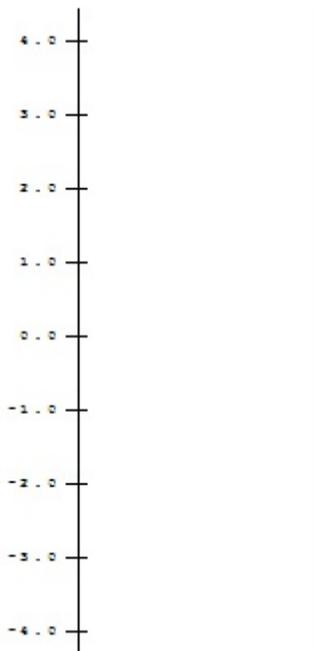
5. Suppose f is a linear function with $f(1) = 3$ and $f(3) = -1$.
- Use a focus point to find $f(0)$.



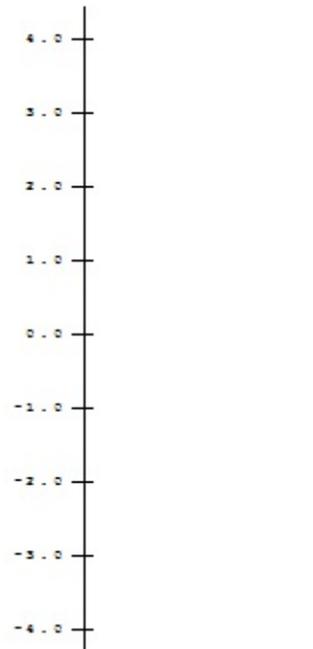
- Use a focus point to find x where $f(x) = 0$.

6. Suppose f is a linear function with $f(x) = 4x - 3$.

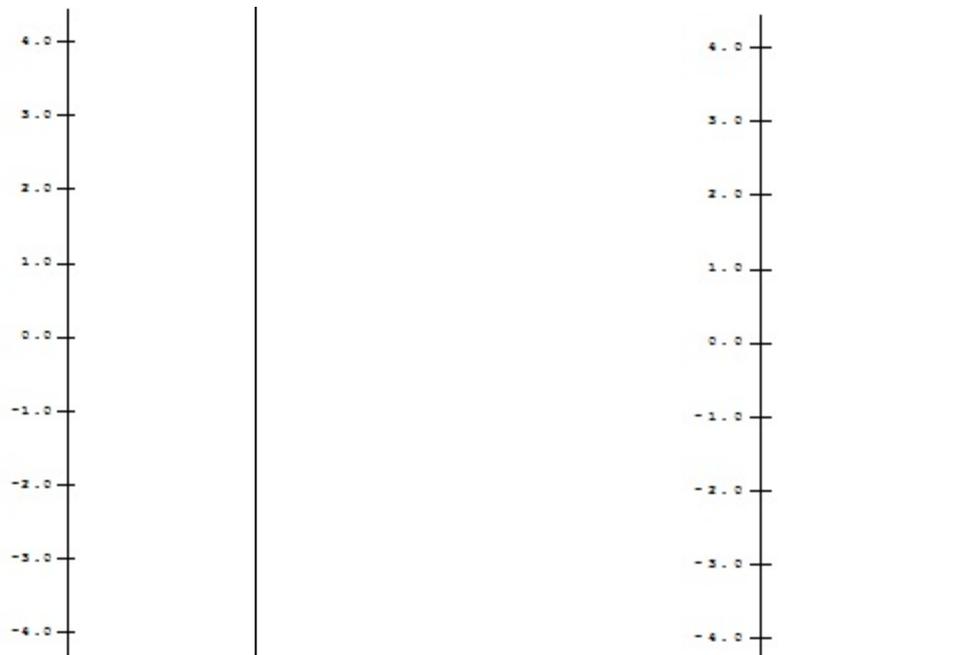
- Sketch a mapping diagram for considering whether $\lim_{x \rightarrow 1} f(x) = 2$ with $\epsilon = \frac{1}{2}$ and $\delta = 0.2$.



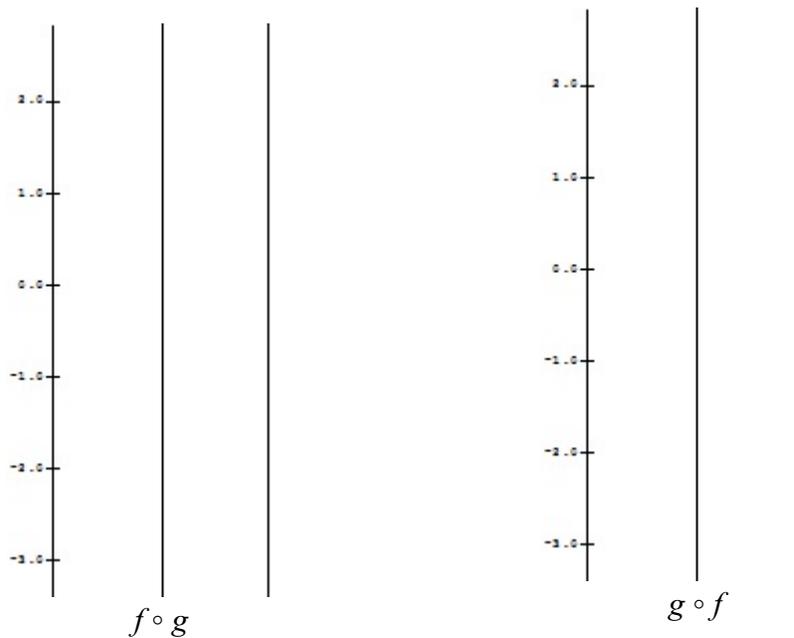
- Sketch a mapping diagram for considering whether $\lim_{x \rightarrow 1} f(x) = 1$ with $\epsilon = \frac{1}{2}$ and $\delta = 0.1$.



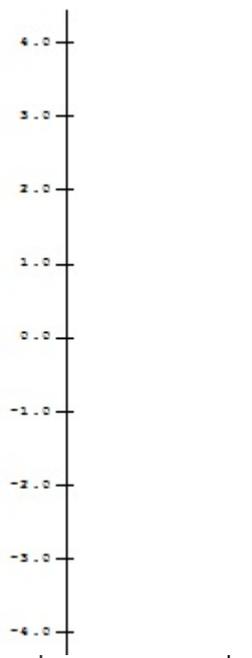
7. Let $f(x) = x^2 - 1$. Visualize an estimation of the derivative $f'(1)$ as a focus point and derivative "vector" on a mapping diagram using $\Delta x = \pm 0.1$.



8. Let $f(x) = 2x$ and $g(x) = -3x + 1$. Visualize the composition of linear functions $f \circ g$ and $g \circ f$ using mapping diagrams.



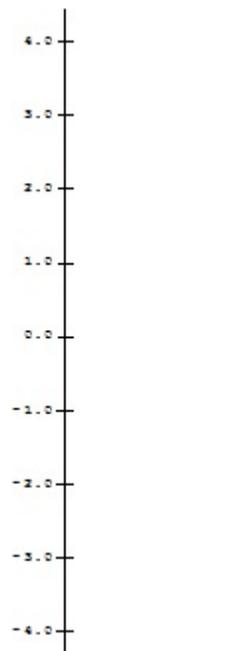
9. Let $f(x) = x^2 - 1$. Use a mapping diagram to visualize estimating the values of $f(1.1)$ and $f(0.9)$ with the differential. [Use $dx = \pm 0.1$, near the value for $x=1$ where $f(1) = 0$, and $dy = f'(1) * dx$.]



10. Complete the following table to estimate of the solution $f(2)$ of the following initial value problem by Euler's method with $n = 4$ ($\Delta x = 1/2$). Use a mapping diagram to visualize the result.

$$\frac{dy}{dx} = f'(x) = 2x - 1 \text{ with } f(0) = 1.$$

| x | $f(x)$ | $\frac{dy}{dx} = f'(x) = 2x - 1$ | $dy = f'(x)dx = (2x - 1)dx$ |
|-----|--------|----------------------------------|-----------------------------|
| 0 | 1 | | |
| 1/2 | | | |
| 1 | | | |
| 3/2 | | | |
| 2 | | | |

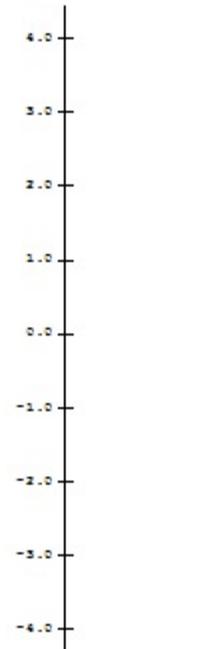


11.

a. Complete the following table to estimate $\int_0^2 2t-1 dt$ by an Euler's sum with $n = 4$ ($\Delta t = 1/2$).

Use a mapping diagram to visualize the result.

| x | $\int_0^x 2t-1 dt$ | $P(t)=2t-1$ | $P(t)\Delta t=(2t-1)\Delta t$ |
|-----|--------------------|-------------|-------------------------------|
| 0 | | | |
| 1/2 | | | |
| 1 | | | |
| 3/2 | | | |
| 2 | | | |



b. Suppose f is a solution to $\frac{dy}{dt}=f'(t)=2t-1$.

Use the estimate for $\int_0^2 2t-1 dt$ to estimate $f(2) - f(0)$.

c. Discuss the connection of this estimate to the mapping diagram and problem 11.
