Visualizing Quadratic, Cubic, and Quartic Equation Solutions: An Introduction to Complex Numbers, Functions, and Mapping Diagrams

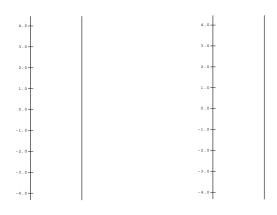
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1.

a. Complete the following tables for m(x) = 2x and s(x) = x + 1

х	m(x) = 2x	s(x) = x + 1
2		
1		
0		
-1		
-2		

b. Using the data from part a), on separate diagrams sketch mapping diagrams for m(x) = 2x and s(x) = x+1



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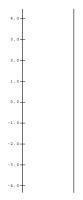
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- 2. Let  $q(x) = x^2$ .
- a. Complete the following table for  $q(x) = x^2$ .

х	$q(x) = x^2$
2	
1	
0	
-1	
-2	

b. Using the data from part a), sketch a mapping diagram for  $q(x) = x^2$ .



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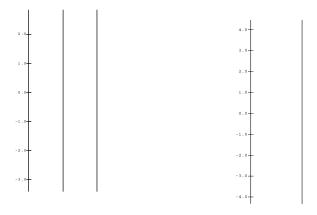
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3.

a. Complete the following table for the composite function f(x) = s(m(x)) = 2x + 1.

х	m(x) = 2x	s(m(x)) = 2 x + 1
2		
1		
0		
-1		
-2		

- b. Use the table and the previous sketches of 1.b to draw a composite sketch of the mapping diagram with 3 axes for the composite function f(x) = s(m(x)) = 2x + 1
- c. Draw a sketch for the mapping diagram with 2 axes of f(x) = 2x + 1.



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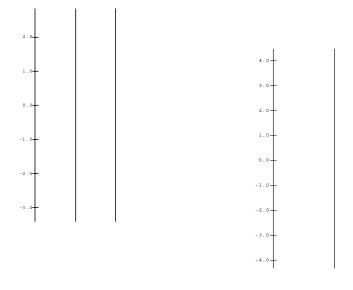
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- 4. Let  $q(x) = x^2$  and  $R(x) = s(q(x)) = x^2 + 1$ .
  - a. Complete the following tables for  $q(x) = x^2$  and  $R(x) = s(q(x)) = x^2 + 1$

х	$q(x) = x^2$	$R(x) = s(q(x)) = x^2 + 1$
2		
1		
0		
-1		
-2		

b. Using the data from part a), on separate diagrams sketch mapping diagrams for the composition  $R(x) = s(q(x)) = x^2 + 1$  with three axes and then two axes.



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## 5. Solving Equations:

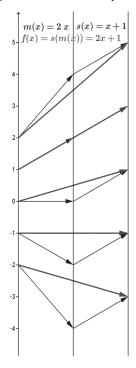
 Use a standard algebraic approach to solve the following equation. Show all steps. Check your answer.

$$2x + 1 = 5$$
.

Work:

# Check:

b. On the mapping diagram below indicate by adding and circling numbers and arrows how the diagram visualizes the work in your algebraic solution of 2x + 1 = 5.



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- 6. Solving  $2(x-3)^2 + 1 = 9$  with a mapping diagram.
  - a. Express  $f(x) = 2(x-3)^2 + 1$  as composition of core linear and quadratic functions. f(x) = h(m(q(x(x)))) where

h(x) =	
m(x) =	
q(x) =	
7 ( v) -	

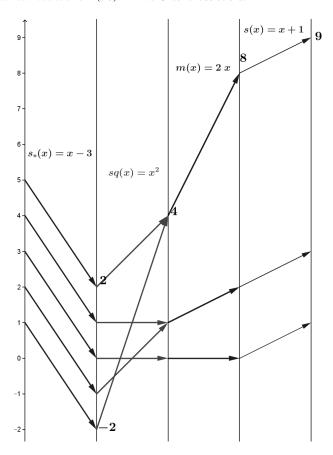
b. Sketch a mapping diagram for f as a composition

	teten a mapping an	agrain for j as a co.	inposition.	
9-				
8-				
7-				
6-				
5-				
4-				
3-				
2-				
1-				
0-				
-1-				
-2-				

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c. On the mapping diagram below indicate by circling numbers and arrows how the diagram visualizes the solution of  $2(x-3)^2 + 1 = 9$ . Check the solutions.



Check:

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- 7. Let  $f(z) = z^2 + 1$ .
  - a. Complete the following table for *f*:

f (a+bi)	-1	0	1
i	f(-1 + i) =	$f(i) = \int$	f(1+i) = 1+2i
0	f(-1) = 2	f(0) = 1	f(1) = 2
-i	f(-1 - i) =	f(-i) =	f(1 - i) =

b. Sketch a mapping diagram for the table data below on the pair of complex planes.

